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# Common Calculus Mistakes

## Definite Integral

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Some problems provide the opportunity for more than one mistake.

### The Goal

Find

$$\int_0^2 e^{-x} dx$$

### The Mistakes

Find the mistakes:

1.

$$\int_0^2 e^{-x} dx = e^{-x} \Big|_0^2 = e^{-2} - e^0 = e^{-2} - 1$$

Need a hint? Look carefully at the red part:

$$\int_0^2 e^{-x} dx = e^{-x} \Big|_0^2 = e^{-2} - e^0 = e^{-2} - 1$$

2.

$$\int_0^2 e^{-x} dx = -e^{-x} \Big|_0^2 = -e^{-2} + (-e^0) = -e^{-2} - 1$$

Need a hint? Look carefully at the red part:

$$\int_0^2 e^{-x} dx = -e^{-x} \Big|_0^2 = -e^{-2} + (-e^0) = -e^{-2} - 1$$

### A Correct Solution

$$\int_0^2 e^{-x} dx = -e^{-x} \Big|_0^2 = -e^{-2} - (-e^0) = -e^{-2} + 1 = 1 - e^{-2}$$

### Explanations

In the first mistake the antiderivative is computed incorrectly - the negative sign is needed.

In the second mistake a common sign error is made. If  $F(x)$  is an antiderivative of the integrand (the function in the integral), the value of the definite integral from  $a$  to  $b$  is  $F(b) - F(a)$ , which applies *even if  $F(x)$  has a minus sign in front of it*. So if  $F(x) = -e^{-x}$ , then  $F(b) - F(a) = (-e^{-b}) - (-e^{-a}) = e^{-a} - e^{-b}$ .